

CMSC201

Computer Science I for Majors

Lecture 22 – Data Representation

Last Class We Covered

- Sorting
 - Bubble
 - Selection
 - Quick
- Searching
 - Linear
 - Binary

Any Questions from Last Time?

Today's Objectives

- To understand how data is represented and stored in memory
 - Binary numbers
 - Hexadecimal numbers
 - Converting
 - Binary to Decimal
 - Decimal to Binary
 - ASCII

Binary Numbers

Binary Numbers

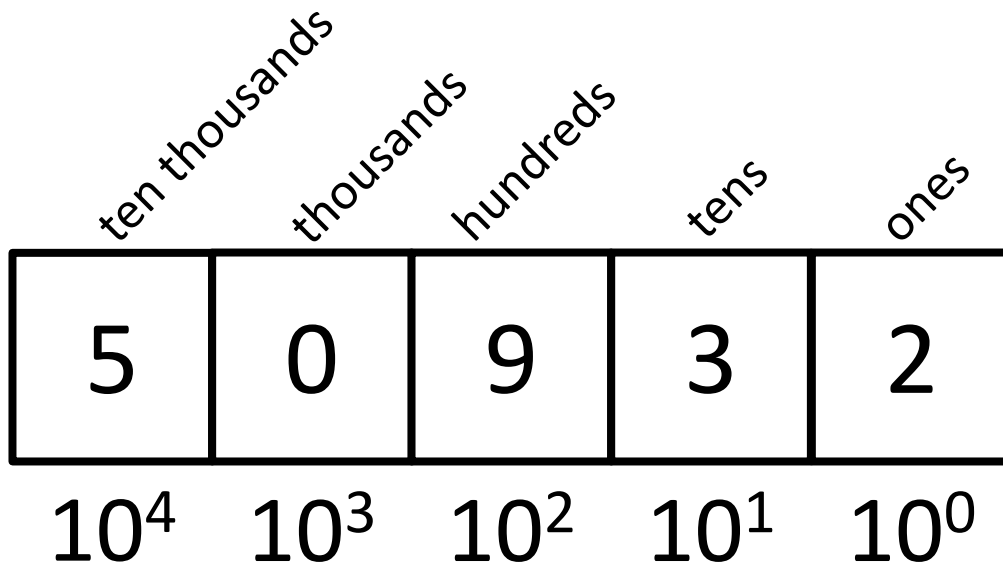
- Computers store all information (code, text, images, sound,) as a binary representation
 - “Binary” means only two parts: 0 and 1
- Specific formats for each file help the computer know what type of item/object it is
- But why use binary?

Decimal vs Binary

- Why do we use decimal numbers?
 - Ones, tens, hundreds, thousands, etc.
- But computers don't have fingers...
 - What do they have instead?
- They only have two states: “on” and “off”

Decimal Example

- How do we represent a number like 50,932?



$$\begin{array}{r}
 2 \times 10^0 = 2 \\
 3 \times 10^1 = 30 \\
 9 \times 10^2 = 900 \\
 0 \times 10^3 = 0000 \\
 5 \times 10^4 = 50000 \\
 \hline
 \text{Total: } 50932
 \end{array}$$

Decimal uses 10 digits, so...

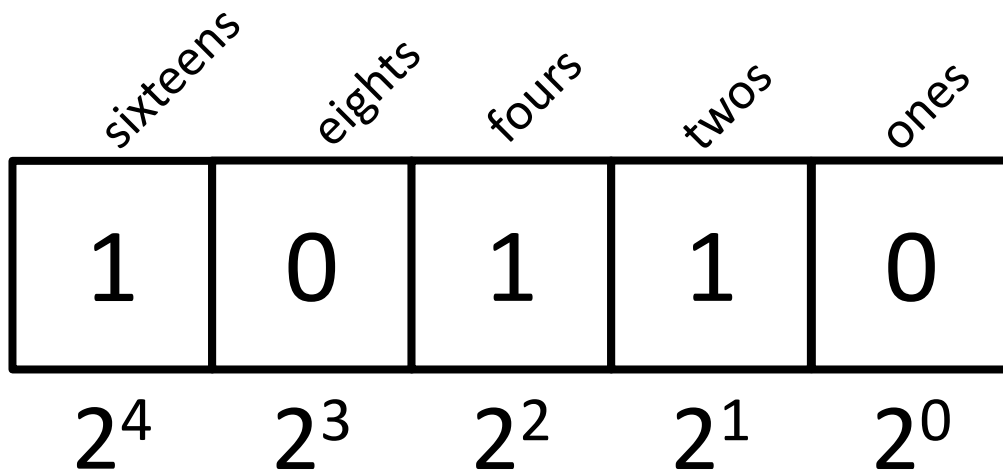
Another Decimal Example

6	7	4	9	3
10^4	10^3	10^2	10^1	10^0
10000	1000	100	10	1
60000	7000	400	90	3

$$60000 + 7000 + 400 + 90 + 3 = 67493$$

Binary Example

- Let's do the same with 10110 in binary



$$\begin{array}{r}
 0 \times 2^0 = 0 \\
 1 \times 2^1 = 2 \\
 1 \times 2^2 = 4 \\
 0 \times 2^3 = 0 \\
 1 \times 2^4 = 16 \\
 \hline
 \text{Total: } 22
 \end{array}$$

Binary uses 2 digits, so our base isn't 10, but...

Binary to Decimal Conversion

- Step 1: Draw Conversion Box
- Step 2: Enter Binary Number
- Step 3: Multiply
- Step 4: Add

1	0	0	0	1	1	0	1
2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
128	64	32	16	8	4	2	1
128	0	0	0	8	4	0	1

$$128 + 0 + 0 + 0 + 8 + 4 + 0 + 1 = 141$$

Exercise: Converting From Binary

- What are the decimals equivalents of...

101


1111

100000

101010

0010 1010

1000 0000



Longer binary numbers are often broken into blocks of four digits for the sake of readability

Exercise: Converting From Binary

- What are the decimals equivalents of...

$$101 = 4 + 0 + 1 = 5$$

$$1111 = 8 + 4 + 2 + 1 = 15$$

$$100000 = 32 + 0 + 0 + 0 + 0 + 0 = 32$$

$$101010 = 32 + 0 + 8 + 0 + 2 + 0 = 42$$

$$0010 \ 1010 = 32 + 0 + 8 + 0 + 2 + 0 = 42$$

$$1000 \ 0000 = 128 + \dots + 0 + 0 = 128$$

Decimal to Binary Conversion

- Step 1: Draw Conversion Box
- Step 2: Compare decimal to highest binary value
- Step 3: If binary value is smaller, put a 1 there and subtract the value from the decimal number
- Step 4: Repeat until 0

Convert 163 to binary

2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
128	64	32	16	8	4	2	1
1	0	1	0	0	0	1	1

$$163 - 128 = 35$$

$$35 - 32 = 3$$

$$3 - 2 = 1$$

$$1 - 1 = 0$$

Converting to Binary

- What are the binary equivalents of...

9

27

68

216

255

Converting to Binary

- What are the binary equivalents of...

$$9 = 1001 \text{ (or } 8+1)$$

$$27 = 0001 \ 1011 \text{ (or } 16+8+2+1)$$

$$68 = 0100 \ 0100 \text{ (or } 64+4)$$

$$216 = 1101 \ 1000 \\ \text{(or } 128+64+16+8)$$

$$255 = 1111 \ 1111 \\ \text{(or } 128+64+32+16+8+4+2+1)$$

Binary Tips and Tricks

- Some “sanity checking” rules for conversions:
 1. Binary can only be 1 or 0
 - If you get “2” of something, it’s wrong
 2. Odd numbers must have a 1 in the ones column
 - Why? (And what’s the rule for even numbers?)
 3. Each column’s value is the sum of all of the previous columns (to the right) plus one
 - In decimal, what column comes after 999?

Hexadecimal Numbers

Decimal Representation

- Decimal uses 10 digits
 - Decimal, *deci* = 10
 - The digits used are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9

ten millions	millions	hundred thousands	ten thousands	thousands	hundreds	tens	ones
9	8	7	5	4	2	1	0
10^7	10^6	10^5	10^4	10^3	10^2	10^1	10^0

Binary Representation

- Binary uses 2 digits
 - Binary, $bi = 2$
 - The digits used are 0 and 1



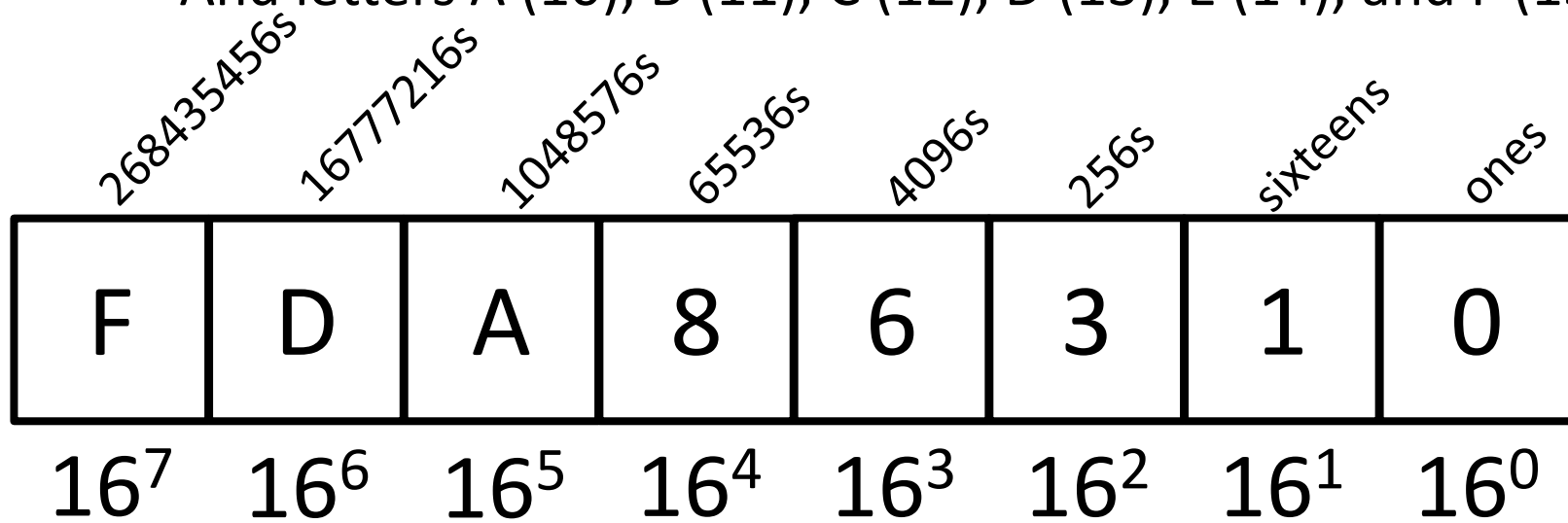
Hexadecimal Representation

- Hexadecimal (or just "hex") uses 16 digits
 - Hexadecimal $\text{hex} = 8 \text{ plus } 8 = 10 \rightarrow 16$
 - The digits used are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9
 - And letters A (10), B (11), C (12), D (13), E (14), and F (15)

F	D	A	8	6	3	1	0
16^7	16^6	16^5	16^4	16^3	16^2	16^1	16^0

Hexadecimal Representation

- Hexadecimal (or just “hex”) uses 16 digits
 - Hexadecimal, *hex* = 6 plus *deci* = 10 → 16
 - The digits used are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9
 - And letters A (10), B (11), C (12), D (13), E (14), and F (15)



Hex to Binary Conversion

- A hexadecimal digit can be easily represented as four digits of binary (with leading zeros)

Hex	Binary	Hex	Binary	Hex	Binary	Hex	Binary
0	0000	4	0100	8	1000	C	1100
1	0001	5	0101	9	1001	D	1101
2	0010	6	0110	A	1010	E	1110
3	0011	7	0111	B	1011	F	1111

- This makes conversion very simple
 - **7A0F** becomes **0111 1010 0000 1111**
 - **1100 0010 0110 1001** becomes **C269**

Hex to Decimal Conversion

- Possible to convert between decimal and hex
 - But it requires calculating out multiples of 16
- Simpler to make a “side trip” to binary as an in-between step when converting
 - 240 becomes **1111 0000** becomes **F0**
 - **F0** is equal to $(15 * 16^1) + (0 * 16^0) = 240 + 0 = 240$
 - **7D** becomes **0111 1101** becomes 125
 - **7D** is equal to $(7 * 16^1) + (13 * 16^0) = 112 + 13 = 125$

Number System Notation

- Because number systems share a subset of the same digits, it may be confusing which is which
 - For example, what is the value of 10?
 - In decimal it's 10, in binary it's 2, and in hex it's 16
- To prevent this, numbers may often be prefixed with **0b**, **0d**, or **0x** (binary, decimal, hex):
 - **0b1100** is binary, and has a value of 12
 - **0x15** is hexadecimal, and has a value of 21

ASCII Values

ASCII Values

- ASCII is how text is represented in computers
 - Just like binary is how numbers are represented
- In ASCII, every character has a unique, individual numerical code
 - Lowercase and uppercase characters are separate
 - Codes go from 0 to 127
 - Why 127?

ASCII TABLE

Decimal	Hex	Char	Decimal	Hex	Char	Decimal	Hex	Char	Decimal	Hex	Char
0	0	[NULL]	32	20	[SPACE]	64	40	@	96	60	`
1	1	[START OF HEADING]	33	21	!	65	41	A	97	61	a
2	2	[START OF TEXT]	34	22	"	66	42	B	98	62	b
3	3	[END OF TEXT]	35	23	#	67	43	C	99	63	c
4	4	[END OF TRANSMISSION]	36	24	\$	68	44	D	100	64	d
5	5	[ENQUIRY]	37	25	%	69	45	E	101	65	e
6	6	[ACKNOWLEDGE]	38	26	&	70	46	F	102	66	f
7	7	[BELL]	39	27	'	71	47	G	103	67	g
8	8	[BACKSPACE]	40	28	(72	48	H	104	68	h
9	9	[HORIZONTAL TAB]	41	29)	73	49	I	105	69	i
10	A	[LINE FEED]	42	2A	*	74	4A	J	106	6A	j
11	B	[VERTICAL TAB]	43	2B	+	75	4B	K	107	6B	k
12	C	[FORM FEED]	44	2C	,	76	4C	L	108	6C	l
13	D	[CARRIAGE RETURN]	45	2D	-	77	4D	M	109	6D	m
14	E	[SHIFT OUT]	46	2E	.	78	4E	N	110	6E	n
15	F	[SHIFT IN]	47	2F	/	79	4F	O	111	6F	o
16	10	[DATA LINK ESCAPE]	48	30	0	80	50	P	112	70	p
17	11	[DEVICE CONTROL 1]	49	31	1	81	51	Q	113	71	q
18	12	[DEVICE CONTROL 2]	50	32	2	82	52	R	114	72	r
19	13	[DEVICE CONTROL 3]	51	33	3	83	53	S	115	73	s
20	14	[DEVICE CONTROL 4]	52	34	4	84	54	T	116	74	t
21	15	[NEGATIVE ACKNOWLEDGE]	53	35	5	85	55	U	117	75	u
22	16	[SYNCHRONOUS IDLE]	54	36	6	86	56	V	118	76	v
23	17	[ENG OF TRANS. BLOCK]	55	37	7	87	57	W	119	77	w
24	18	[CANCEL]	56	38	8	88	58	X	120	78	x
25	19	[END OF MEDIUM]	57	39	9	89	59	Y	121	79	y
26	1A	[SUBSTITUTE]	58	3A	:	90	5A	Z	122	7A	z
27	1B	[ESCAPE]	59	3B	;	91	5B	[123	7B	{
28	1C	[FILE SEPARATOR]	60	3C	<	92	5C	\	124	7C	
29	1D	[GROUP SEPARATOR]	61	3D	=	93	5D]	125	7D	}
30	1E	[RECORD SEPARATOR]	62	3E	>	94	5E	^	126	7E	~
31	1F	[UNIT SEPARATOR]	63	3F	?	95	5F	_	127	7F	[DEL]

“control”
characters

ASCII TABLE

uppercase
letters

Decimal	Hex	Char
0	0	[NULL]
1	1	[START OF HEADING]
2	2	[START OF TEXT]
3	3	[END OF TEXT]
4	4	[END OF TRANSMISSION]
5	5	[ENQUIRY]
6	6	[ACKNOWLEDGE]
7	7	[BELL]
8	8	[BACKSPACE]
9	9	[HORIZONTAL TAB]
10	A	[LINE FEED]
11	B	[VERTICAL TAB]
12	C	[FORM FEED]
13	D	[CARRIAGE RETURN]
14	E	[SHIFT OUT]
15	F	[SHIFT IN]
16	10	[DATA LINK ESCAPE]
17	11	[DEVICE CONTROL 1]
18	12	[DEVICE CONTROL 2]
19	13	[DEVICE CONTROL 3]
20	14	[DEVICE CONTROL 4]
21	15	[NEGATIVE ACKNOWLEDGE]
22	16	[SYNCHRONOUS IDLE]
23	17	[ENG OF TRANS. BLOCK]
24	18	[CANCEL]
25	19	[END OF MEDIUM]
26	1A	[SUBSTITUTE]
27	1B	[ESCAPE]
28	1C	[FILE SEPARATOR]
29	1D	[GROUP SEPARATOR]
30	1E	[RECORD SEPARATOR]
31	1F	[UNIT SEPARATOR]

Decimal	Hex	Char
32	20	[SPACE]
33	21	!
34	22	"
35	23	#
36	24	\$
37	25	%
38	26	&
39	27	'
40	28	(
41	29)
42	2A	*
43	2B	+
44	2C	,
45	2D	-
46	2E	.
47	2F	/
48	30	0
49	31	1
50	32	2
51	33	3
52	34	4
53	35	5
54	36	6
55	37	7
56	38	8
57	39	9
58	3A	:
59	3B	;
60	3C	<
61	3D	=
62	3E	>
63	3F	?

Decimal	Hex	Char
64	40	@
65	41	A
66	42	B
67	43	C
68	44	D
69	45	E
70	46	F
71	47	G
72	48	H
73	49	I
74	4A	J
75	4B	K
76	4C	L
77	4D	M
78	4E	N
79	4F	O
80	50	P
81	51	Q
82	52	R
83	53	S
84	54	T
85	55	U
86	56	V
87	57	W
88	58	X
89	59	Y
90	5A	Z
91	5B	[
92	5C	\
93	5D]
94	5E	^
95	5F	_

Decimal	Hex	Char
96	60	`
97	61	a
98	62	b
99	63	c
100	64	d
101	65	e
102	66	f
103	67	g
104	68	h
105	69	i
106	6A	j
107	6B	k
108	6C	l
109	6D	m
110	6E	n
111	6F	o
112	70	p
113	71	q
114	72	r
115	73	s
116	74	t
117	75	u
118	76	v
119	77	w
120	78	x
121	79	y
122	7A	z
123	7B	{
124	7C	
125	7D	}
126	7E	~
127	7F	[DEL]

symbols &
numbers

lowercase
letters

Comparing Strings

- The values of the ASCII characters are used when comparing strings together
 - Which can lead to some “weird” results

```
>>> "cat" < "dog"
```

```
True
```

```
>>> "cat" < "Dog"
```

```
False
```

```
>>> "DOG" < "dog"
```

```
True
```



?



More on Comparing Strings

- Gets even more complex when you start adding in numbers and symbols

```
>>> "2" < "one"
```

```
True
```

```
>>> "good?" < "good!"
```

```
False
```

```
>>> "UK" < "U.K."
```

```
False
```

Rules for Comparisons

- To avoid (some) of these issues:
- Always use `.lower()` for comparing strings
- Pay attention to symbols
 - *e.g.*, spaces, hyphens, punctuation, etc.
 - Either remove them, or keep them in mind as part of the order

ASCII Characters to ASCII Values

- We can convert between ASCII characters and their values using `ord()` and `chr()`
- The `ord()` function takes in a single character, and returns its ASCII value
- The `chr()` function takes in an integer, and returns its ASCII character

Using `chr()` and `ord()`

```
>>> chr(65)
```

```
'A'
```

```
>>> chr(65+32)
```

```
'a'
```

```
>>> ord('?')
```

```
63
```

```
>>> ord("d")
```

```
100
```

```
>>> ord("e")
```

```
101
```

Project 3

Project 3 Tips

- Hopefully you have started by now!
 - Work on it a little everyday
- You have been given some solved puzzles
 - Which means you don't need a working `solve()` to test the other parts of your project
 - Just load in the solution from the file
- Solve the puzzle once, and store the solved puzzle to use it later in your code
 - Don't resolve it every time you need it
- Make your own puzzles to test!

Project 3 and Deep Copy

- You will need to make a deep copy of the 2D list used to hold your Sudoku board
 - Simply using `new = old[:]` will not work
- We recommend making a function to do this
 - Test that your function works before using it
- Do **NOT** use the built-in `deepcopy()` function, or you will lose major points!!!

Do Not Cheat on Project 3

- Yes, this project has solutions on the internet
 - Yes, we have copies of all of them
 - Yes, we will go looking for new ones after it's due
- Yes, you could pay someone else to do it
 - Yes, we know of the sites where you can get this done
 - Yes, we will spot “elegant” code that you didn't write
- Yes, there are libraries to deep copy in python
 - Yes, you will get points off for using them
 - You should not be importing anything for this project

Questions?

Announcements

- Project 3
 - Design is due Tuesday, December 4th
 - Project is due Tuesday, December 11th
- Final exam is when?
 - Friday, December 14th from 6 to 8 PM
 - Locations will be posted on the course website
 - Common final